

Optical Emission Spectroscopy Study of Competing Phases of Electrons in the Second Landau Level

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Quantum phases of electrons in the filling factor range $2 \leq \nu \leq 3$ are probed by the weak optical emission from the partially populated second Landau level and spin wave measurements. Observations of optical emission include a multiplet of sharp peaks that exhibit a strong filling factor dependence. Spin wave measurements by resonant inelastic light scattering probe breaking of spin rotational invariance and are used to link this optical emission with collective phases of electrons. A remarkably rapid interplay between emission peak intensities manifests phase competition in the second Landau level.

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Ultraclean two-dimensional electron systems in the presence of high perpendicular magnetic fields B are a source of unexpected and fascinating quantum many-body physics that arises from the strong electron interactions combined with a reduction in dimensionality. When B is high enough for all electrons to occupy the lowest ($N = 0$) Landau level (LL), the many-electron system forms liquids of the fractional quantum Hall effect (FQHE). When B is such that electrons fill states in higher ($N \geq 2$) LLs, electrons form quantum phases referred to as stripe and bubble phases, which lead to transport anisotropy and reentrant integer quantum Hall effect (RIQHE) states [1–3]. The unique electron-electron interactions in the $N = 1$ LL result in the presence of RIQHE states and stripe phases in addition to even- and odd-denominator FQHE states [3,4]. FQHE states in the second ($N = 1$) LL exhibit even-denominator states such as the one at $\nu = 5/2$ [5,6], which is predicted to have non-Abelian excitations [7–14], have recently been studied by NMR [15,16], by light scattering methods [17,18], and in two-subband systems [19]. It has been predicted that the less studied FQHE state at $\nu = 2 + 1/3 = 7/3$ could possess exotic quasiparticles in which composite fermions are dressed by a cloud of neutral excitations [20]. Since FQHE liquids as well as bubble and stripe phases can serve as ground states, the $N = 1$ LL is home to a striking competition between quantum phases [21].

The interplay of anisotropic phases with FQHE liquids in the second LL has been studied by introduction of in-plane magnetic fields [3,22–25]. These experiments provide

evidence that anisotropic smectic- or nematiclike phases with broken full rotational invariance coexist with quantum Hall liquids [26–30]. The large anisotropy induced in the system at the FQHE states at $\nu = 5/2$ and $\nu = 7/3$ by relatively small in-plane magnetic fields [22–24] supports interpretations in terms of a new state of electron matter with FQHE states that occur in the environment of a nematic stripe phase [30–32].

We report optical emission experiments that probe quantum phases that emerge in the second LL of an ultraclean 2D electron system. The optical recombination is from transitions across conduction to valence band states from electrons that partially populate the $N = 1$ LL. This emission, while much weaker than the one originating in the $N = 0$ LL [see Figs. 1(c) and 1(d)], displays a marked dependence on filling factor, which uncovers competing and overlapping quantum phases in the range $2 < \nu < 3$.

Links between optical emission and emerging quantum phases are established by comparing optical emission with the long-wavelength spin wave obtained by resonant inelastic light scattering (RILS). At ferromagnetic quantum Hall states such as $\nu = 3$, all spins are aligned, and the long wavelength spin wave occurs at the bare Zeeman energy, in agreement with the Larmor theorem [33]. The departure from the Larmor theorem for $\nu < 3$ is regarded as the evidence of formation of spin textures that break the full rotational invariance of the 2D electron system due to the combined effects of Coulomb interactions and disorder [17,18,34].

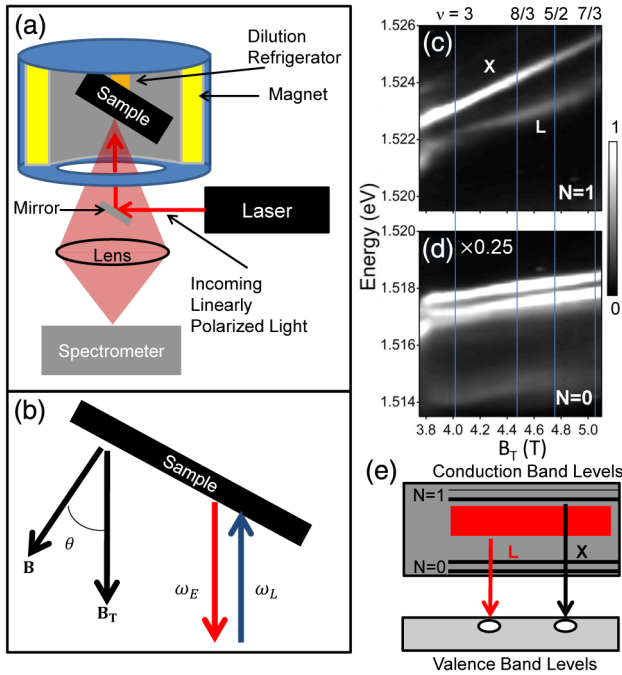


FIG. 1. (a) Experimental setup with bottom optical access in the dilution refrigerator. (b) Schematic description of the experimental geometry showing incident and emitted photons and the tilt angle θ of the sample. The total magnetic field B_T and the perpendicular component B are also shown. (c) Energy vs B_T observed in optical emission spectra from the $N = 1$ LL in the filling factor range $2 \leq \nu \leq 3$ for sample A. The intensity is shown in gray scale. The band labeled X is linearly dispersed in B_T . L is the redshifted optical emission that is considered in the main text. (d) Energy vs B_T plot for optical emission spectra from the $N = 0$ LL in the range $2 \leq \nu \leq 3$ for sample A. (e) Schematic description of optical emission transitions that originate in the $N = 1$ LL.

The emission from the $N = 1$ LL displays two major components, a singlet with linear magnetic field dependence and a redshifted multiplet with a striking dependence on filling factor. An investigation of links between optical emission and spin waves in RILS spectra allows us to link the peaks in the redshifted optical emission to quantum phases in the $N = 1$ LL. The wide ranges of filling factors over which these phases exist, together with the absence of a clear temperature dependence for $T \leq 300$ mK, indicates that these are not FQHE or RIQHE phases, but, we surmise, phases that coexist with them.

The filling factor dependence of the redshifted optical emission is particularly striking in the filling factor range $2 \lesssim \nu \lesssim 2.5$, where three distinct peaks display rapid changes in intensity with magnetic field in a narrow filling factor range. Softening of the spin wave from the Zeeman energy in this filling factor range is similar to the effect reported in the filling factor range $2/3 < \nu < 1$, which was interpreted as arising from the appearance of spin textures in the ground state [35]. Measurements of the spin wave by

RILS thus allow us to probe the spin rotational invariance of the competing phases observed through optical emission.

The 2D electron system is realized in two samples each with a symmetrically doped single GaAs/AlGaAs quantum well of width 300 Å [36,37]. The charge carrier density in the lower density sample A is $2.92 \times 10^{11} \text{ cm}^{-2}$, measured in transport experiments, and the carrier mobility is $23.9 \times 10^6 \text{ cm}^2/\text{Vs}$ (at 300 mK). The higher density sample B has a density of $3.2 \times 10^{11} \text{ cm}^{-2}$ and mobility of $20 \times 10^6 \text{ cm}^2/\text{Vs}$ (at 300 mK). Samples are mounted on the cold finger of a $^3\text{He}/^4\text{He}$ dilution refrigerator operating at a base temperature below 40 mK and placed in the bore of a 16 T superconducting magnet. Bottom windows are employed for spectroscopy [Fig. 1(a)]. The optical emission spectra are excited by a tunable Ti:sapphire laser at an incident power below $10^{-4} \text{ W}/\text{cm}^2$ and recorded in the backscattering geometry shown in Fig. 1(b). Laser heating at this power density keeps the electron gas temperature below 100 mK at the base temperature of the dilution refrigerator, as demonstrated in Ref. [38]. The excitation wavelength of 800 nm is at a photon energy close to the fundamental optical gap of the GaAs quantum well. The sample is tilted at an angle $\theta = 20^\circ$. The resulting small in-plane component of the magnetic field allows for well-defined FQHE states at $\nu = 5/2$ and $\nu = 7/3$, and also anisotropic phases in the second LL [3,4,22,23]. The filling factor is identified by the strong spin wave in the polarized $\nu = 3$ state as described in the Supplemental Material [39].

The optical emission is well represented by multiple Lorentzians with varying amplitude and nearly constant width (the width itself depending on the particular peak). The results of such line shape analysis in the range $2 \leq \nu \leq 3$ are summarized in Fig. 2(b), which presents peak energies as a function of total magnetic field B_T . The area of each data point is proportional to the integrated intensity of the peak found from a Lorentzian fit such as shown in Fig. 2(a) and normalized by the electron population of the $N = 1$ LL.

Figures 1(c) and 1(d) summarize optical emission results in the range $2 \leq \nu \leq 3$. The emission doublet from the $N = 0$ LL [Fig. 1(d)] is similar to those reported in previous studies [44,45]. The focus here is on the much weaker optical recombination due to transitions that originate from partially populated states in the $N = 1$ LL shown in Fig. 1(c), which displays two major features labeled as X and L. This result is markedly different from the $N = 0$ emission spectra in a range $\nu \leq 1$, where bands disperse linearly in B and display oscillation in energy as a function of ν [46,47].

Figure 2(a) presents a typical optical emission spectrum and resonant Rayleigh scattering (RRS) at $\nu = 2.50$. In the partially populated $N = 1$ LL, RRS identifies the energy of the excitonic transitions between the partially populated conduction band and the valence band [17]. The RRS

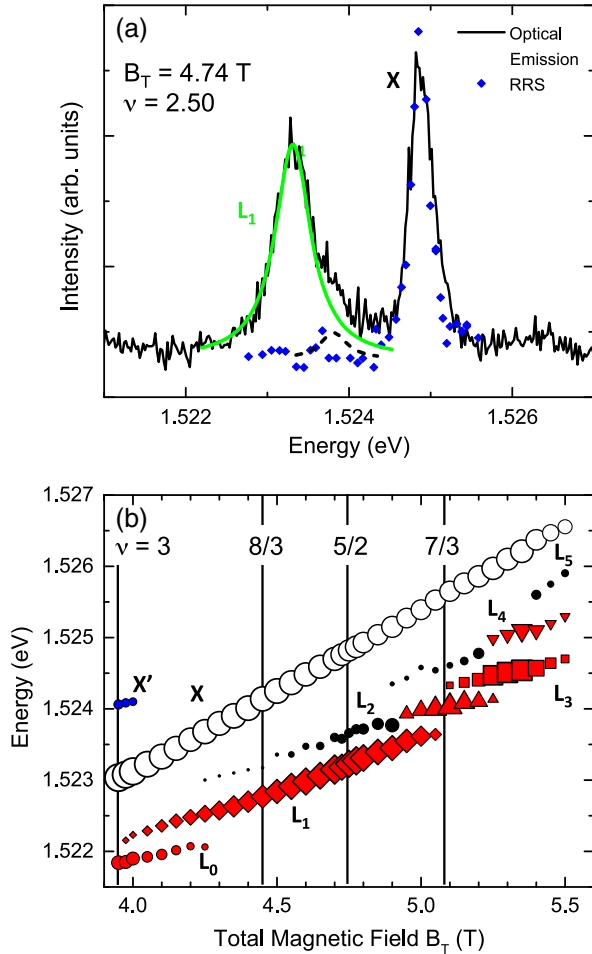


FIG. 2. (a) RRS results overlapped with optical emission for $\nu = 2.50$ from sample A. (b) Energy of the bands in the optical emission from sample A from the $N = 1$ LL as a function of total magnetic field B_T . The area of each data point is proportional to the integrated intensity found from a Lorentzian fit (except in the case of L_0 and L_4 , which appear Gaussian) such as the green curve in (a) and normalized by the electron population of the $N = 1$ LL. The black closed circles indicate low intensity emission with higher uncertainty on its energy, such as the black dashed curve in (a).

measurements reveal the X peak as resulting from excitonic transitions. The energy of the singlet X band has a linear dependence on the perpendicular component of the magnetic field B with a slope of 2.39 ± 0.05 meV/T, illustrated in Fig. 2(b). This value of the slope is close to that of free electrons in GaAs in the $N = 1$ LL. Such magnetic field dependence indicates that the X emission arises from optical transitions at energies that are modified from single particle transition energies of conduction and valence LLs by excitonic interactions and weak coupling to the electron system. The redshifted L emission is a multiplet structure [Fig. 2(a)] that exhibits a strong dependence on filling factor [Fig. 2(b)]. The optical transitions for the L peaks are shown in Fig. 1(e) as redshifted from single-particle

conduction states. The RRS measurements in Fig. 2(a) show that the absorption edge is at the X peak, suggesting that the recombination responsible for the L multiplet consists of lower energy electron states than the X peak.

Figure 3 establishes the link between the redshifted L emission peaks and electron phases near $\nu = 3$. The interplay between the L peaks [Fig. 3(a)] correlates with a softening and collapse of the Zeeman mode [Fig. 3(b)]. At $\nu = 3$, the L emission consists of a singlet peak labeled L_0 [Fig. 3(a)]. The rapid reduction of the L_0 intensity with decreasing filling factor and simultaneous softening of the spin wave clearly indicates that the L_0 emission is characteristic of the integer QHE state at $\nu = 3$. Figures 2(b) and 3(a) illustrate the emergence of a new peak L_1 around $\nu = 2.96$, which becomes the dominant feature of the L emission for $\nu \lesssim 2.9$. Figure 3(b) shows a strong Zeeman mode at $\nu = 3$ that rapidly decreases in energy and collapses as the L_1 peak gains intensity. The correlation between the emission and spin wave spectra links the appearance of the L_1 band to the emergence of a new phase in the partially populated $N = 1$ LL. The softening and collapse of the spin wave away from $\nu = 3$ indicates the presence of spin textures that break the full rotational invariance necessary to support spin waves at the Zeeman energy.

The most striking feature of the L multiplet is the interplay between the intensities of L_1 , L_2 , and L_3 peaks in the vicinity of $\nu = 7/3$ (Fig. 4). As B_T increases and ν approaches $7/3$, the L_1 component loses intensity and disappears from the spectra for $\nu \lesssim 2.32$. Simultaneously, the L_2 band, which becomes well defined for $\nu < 5/2$ [Fig. 2(b)], increases in intensity, as seen in Fig. 4(a). A

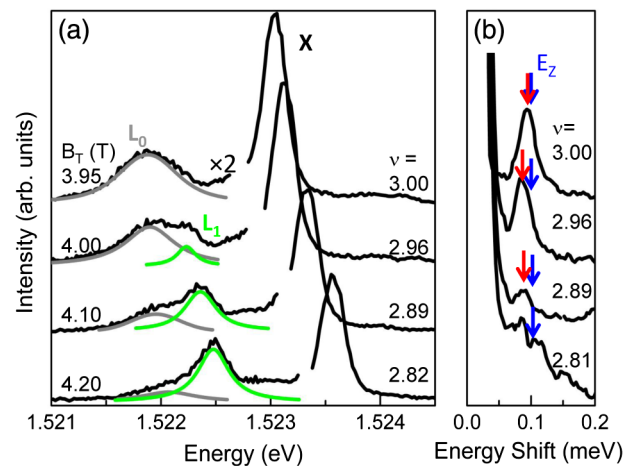


FIG. 3. (a) Optical emission and (b) RILS spectra from sample A for filling factors close to 3. The color curves in (a) are fits with Lorentzian functions. The observed spin wave in (b) is indicated with a red arrow and compared to the Zeeman energy (blue arrow). Data shown in (b) were collected during a different cooldown of the dilution refrigerator [18], which results in a small difference in magnetic fields that achieve the same filling factors as (a).

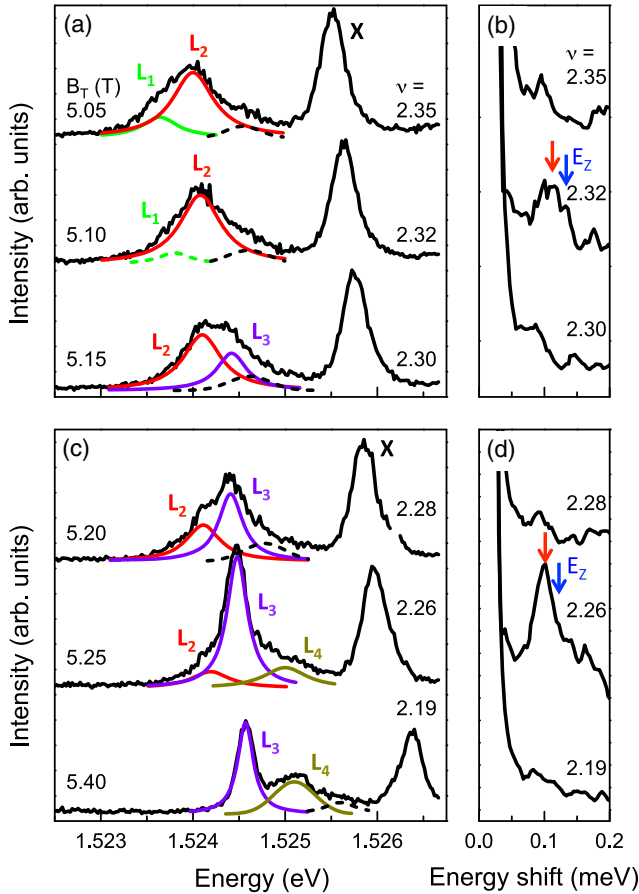


FIG. 4. (a) Optical emission and (b) RILS spectra from sample A for filling factors close to $7/3$. (c) Optical emission and (d) RILS spectra from sample A for a filling factor range where peak L_3 is dominant. The color curves in (a,c) are fits with Lorentzian functions. The observed spin wave in (b,d) is indicated with a red arrow and compared to the Zeeman energy (blue arrow).

similar competition is seen in the results presented in Fig. 4(c), where the intensity of L_3 increases sharply as the intensity of L_2 quickly collapses. RILS spectra display a recovery of the long-wavelength spin waves near $\nu = 7/3$, where the intensity of L_2 is the highest, and at $\nu = 2.26$, where L_3 dominates the multiplet [Figs. 4(b),4(d), and Ref. [18]]. The discernible softening of the spin wave from the Zeeman energy near $\nu = 7/3$ [Fig. 4(b)] and $\nu = 2.26$ [Fig. 4(d)] is similar to the one observed at $\nu < 3$ [Fig. 3(b)]. A similar interpretation to explain the results in Fig. 4 suggests that the softening of the spin wave is evidence that the phases responsible for the L_2 and L_3 emission bands, similar to L_1 , possess spin textures that break the full rotational invariance. This interpretation is consistent with results from anisotropic transport at $\nu = 7/3$ [23]. The L_2 emission fully dominates the redshifted multiplet near $\nu = 7/3$ [Fig. 4(a)] and is thus associated with a quantum phase that is dominant near $\nu = 7/3$.

We vary the temperature to gain additional insights into the nature of the observed quantum phases. The temperature dependence of the optical emission appears to be negligible for $T < 300$ mK for the entire range $2 < \nu < 3$ (see Fig. S4 in the Supplemental Material [39], where sample B is studied). For a large range of filling factors, optical emission does not exhibit a discernible temperature dependence below 650 mK, whereas there is a clear temperature dependence at certain filling factors, notably $\nu = 2.32$ [Fig. S4(b)], for $300 \text{ mK} < T < 650 \text{ mK}$. The fits suggest a competition between L_2 and L_3 , with the L_3 gaining intensity and L_2 shrinking with increasing temperature. This temperature dependence is significantly weaker than that of FQHE and RIQHE [40] and is more similar to the temperature dependence of anisotropic transport at $\nu = 7/3$ [23].

The exploration of optical emission from the partially populated $N = 1$ LL offers new insights into exotic quantum phases that emerge in the filling factor range $2 \leq \nu \leq 3$. The anomalous spin waves that correlate with the presence of L_1 , L_2 , and L_3 emission bands break Larmor theorem, indicating spin textures that lack full spin rotational invariance. These results support a conceptual framework in which the bands of the L multiplet are associated with distinct phases in the partially populated $N = 1$ LL and the interplay in the peak intensities demonstrated in Figs. 4(a) and 4(c) is understood as revealing a sharp competition between phases that occur near filling factors $7/3$ and 2.26 . The rapid changes that occur in the L multiplet for filling factors near the FQHE state at $\nu = 7/3$ suggest a striking competition between quantum ground states that are tuned by remarkably small changes in filling factor. The results demonstrate that optical methods form a powerful tool for the identification and study of exotic quantum phases of electrons in the partially populated $N = 1$ LL.

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